

1. Find all solutions to the equation in the interval  $[0, 2\pi)$ .

a)  $4\cos^2 x = 3$

b)  $\sin x \tan^2 x = \sin x$

c)  $\sin\left(x + \frac{\pi}{6}\right) - \sin\left(x - \frac{\pi}{6}\right) = \frac{1}{2}$

2. Find all solutions to the equation, using your calculator in the interval  $[0, 2\pi)$ . Round to two decimal places.

a)  $\cos 2x + 5\cos x = 2$

b)  $\sin 3x = \sin x$

c)  $5\sin 2x - 12\cos 2x = 0$

3. Find the exact value.

a)  $\sin \frac{\pi}{12}$

b)  $\cos(105^\circ)$

c)  $\sin 60^\circ + \sin 30^\circ$

4. Write the expression as the sine, cosine, or tangent of an angle.

a)  $\frac{\tan 20^\circ - \tan 15^\circ}{1 + \tan 20^\circ \tan 15^\circ}$

b)  $\sin\left(\frac{\pi}{4}\right)\cos\left(\frac{\pi}{6}\right) + \cos\left(\frac{\pi}{4}\right)\sin\left(\frac{\pi}{6}\right)$

c)  $\cos 30^\circ \cos 25^\circ - \sin 30^\circ \sin 25^\circ$

5. Prove the following identities.

a)  $\frac{1+\tan x}{\tan x-1} = \frac{\cot x+1}{1-\cot x}$

b)  $2\sin\theta\cos^3\theta + 2\sin^3\theta\cos\theta = \sin 2\theta$

c)  $(\cos x - \sin x)^2 + (\cos x + \sin x)^2 = 2$

d)  $\tan\left(x + \frac{3\pi}{4}\right) = \frac{\tan x - 1}{1 + \tan x}$

e)  $\frac{\sec^2\theta - 1}{\sin\theta} = \frac{\sin\theta}{1 - \sin^2\theta}$

f)  $\tan^2 x - \sin^2 x = \sin^2 x \tan^2 x$

g)  $\frac{1}{\sec x - 1} + \frac{1}{\sec x + 1} = 2\cot x \csc x$

6. Find  $\sin 2x$  and  $\cos 2x$  given that  $\sin x = \frac{-2}{7}$  and  $\frac{3\pi}{2} < x < 2\pi$ .